

# SECURITY MODELS FOR EVERLASTING PRIVACY

ATHECRYPT 2020

PANAGIOTIS GRONTAS

ARIS PAGOURTZIS

ALEXANDROS ZACHARAKIS

NATIONAL TECHNICAL UNIVERSITY  
OF ATHENS

07.01.2020



<https://eprint.iacr.org/2019/1193>

- Game-based definitions for everlasting privacy
- A new adversarial model
  - ▶ **Powerful** computational capabilities *in the future*
  - ▶ **Extensive** data collection *in the present*
- Contemporary adversary (privacy)
  - ▶ Corrupt voters
  - ▶ Monitor & store communications
  - ▶ Computationally bounded
- Future adversary
  - ▶ Examine past **public** data
  - ▶ Potentially has **insider access** to past **private data** (surveillance - breaking of trust assumptions)
  - ▶ Computationally powerful
- Everlasting privacy variations



# ELECTRONIC VOTING PROPERTIES: VERIFIABILITY



**Aleksander Essex** @aleksessex · Nov 4, 2019

Electronic voting is like betting on a coin toss where you can't inspect the coin, you can't toss the coin, you can't call it in the air, and you most certainly can't see how it landed. I tell you when you lose, and you hand over the money. What? Don't you trust me? 😊

- Voters vote in an adversarial environment (bugs, malice)
- Election authorities and voter devices are **not trusted**

## Checks:

- Cast as intended
- Recorded as cast
- Talled as recorded

Verifiability: voters and auditors check the process

- Individual
- Universal
- Eligibility

Accountability: a stronger form of verifiability

# ELECTRONIC VOTING PROPERTIES: PRIVACY

Standard feature of elections since the 19th century encoded into law

Privacy is **not absolute**: The result reveals information **but no more should leak**

- Secrecy: Encryption & Commitment schemes [CFSY96, Adio8, KZZ15]
- Anonymity: Mixnets [Cha81] & Blind signatures [Cha82]
- Computational & trust assumptions
- Flavors:
  - ▶ Receipt Freeness [BT94]
  - ▶ Coercion Resistance [JCJ05]
  - ▶ Perfect Ballot Secrecy [KY02]
  - ▶ Everlasting Privacy [MN06]



# RELATION OF PRIVACY AND VERIFIABILITY

- To enable verifiability the system must generate evidence
  - ▶ without compromising secrecy
  - ▶ without functioning as a receipt
- Does verifiability without privacy make sense?
  - ▶ Does it really matter if the vote is dictated by a coercer or changed by a corrupted authority?
- You can't have (computational) privacy without individual verifiability [CL18]
  - ▶ Replace votes in order to learn how a targeted voter voted
  - ▶ Voters that check their votes protect the privacy of others
- Integrity is ephemeral, privacy should be everlasting [MNo6]
  - ▶ integrity matters until the loser is convinced

# EVERLASTING PRIVACY = POST SNOWDEN PRIVACY

- Encryption becomes obsolete
  - ▶ Gradually (e.g. Moore's Law, better attacks)
  - ▶ Spectacularly (e.g. practical quantum computing)
- Verifiability → election data widely available
- Voting data can be valuable to a future authoritarian regime
- Resources in Snowden's world:
  - ▶ Advanced computational power
  - ▶ Collected data (e.g. mass surveillance)
  - ▶ Insider data (e.g. political parties)
- Indirect coercion attempt



# EVERLASTING PRIVACY: PREVIOUS WORK I

Formal study  
initiated in [MNo6]

Receipt-Free Universally-Verifiable Voting with  
Everlasting Privacy\*

Tal Moran and Moni Naor\*\*

Department of Computer Science and Applied Mathematics,  
Weizmann Institute of Sciences, Rehovot, Israel

More concrete in  
[MN10]

Split-Ballot Voting:  
Everlasting Privacy With Distributed Trust

TAL MORAN  
Weizmann Institute of Science, Israel  
and  
MONI NAOR  
Weizmann Institute of Science, Israel

Previously hinted in:  
[CFSY96]: Perfectly hiding

Pedersen commitments &  
verifiable secret sharing  
through private channels  
[FOO92]

**Theorem 3 (Privacy).** *Even if the administrator and the counter conspire, they cannot detect the relation between vote  $v_i$  and voter  $V_i$ .*

*Sketch of Proof.* The relation between the voter's identity  $ID_i$  and the ballot  $x_i$  is hidden by the blind signature scheme. The ballot  $x_i$  and the key  $k_i$  are sent through the **anonymous communication channel**. So no one can trace the communication and violate the privacy of the voters. **It is unconditionally secure against tracing the voting.**

Made practical in [HG19]

Blind signatures &  
anonymous channels

### Split ballot voting [MN10]

- Two election authorities
- Votes cast protected using a perfectly hiding commitment scheme
- To tally, the openings are required
- Exchanged computationally protected
- Tallying: Parallel shuffling of commitments and openings between the authorities
- Casting is not anonymous
- Everlasting privacy
  - ▶ the authorities are honest
  - ▶ they do not collaborate
  - ▶ the openings are not made public
- One corrupted authority: computational privacy
- Two corrupted authorities: correctness

## EVERLASTING PRIVACY: PREVIOUS WORK III

Everlasting privacy = information theoretic security against the public view

- [DGA12] Replace Helios exp. ElGamal with Pedersen commitments (openings sent through private channels)
- [CPP13] Commitment Consistent Encryption - use of public/private Bulleting Boards
- [BDV13] Encapsulate as a mixnet
- [ACKR13] Formalization as *practical* everlasting privacy in the applied pi-calculus



Revisiting the **anonymous** channel idea [FOO92] for casting

[LH15] & [LHK16]:

- Public credentials to the Bulletin Board
- (Un)encrypted vote to the Bulletin Board
- Commitment to 1 out of  $n$  voting credentials with ZKPoK
- Follow up: Deniable vote updating for coercion resistance



Anonymous channel: helps with coercion resistance by thwarting forced abstention attack

### [GPZZ19]

- Coercion resistance using real-fake credentials
- All valid credentials posted to BB
- During voting attach a (fake) credential to a blinded ballot
- Election authority marks validity by signing
- All checks are embedded into a variation of blind signatures (PACBS)
- Include ZKPoK for EA's actions provide verifiability

All voting interactions are auditable in the BB

# A GENERIC VOTING SYSTEM - PARTICIPANTS

## Participants:

- Election Authority
- $n$  voters
- $m$  candidates
- Bulletin Board to store all voting related data in a publicly accessible manner



Participants

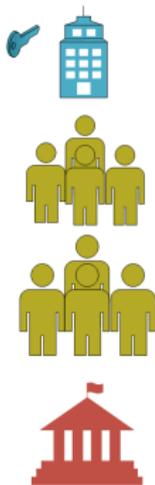
# A GENERIC VOTING SYSTEM - FUNCTIONALITIES

- $(\text{params}, \text{sk}_{\mathcal{E}\mathcal{A}}, \text{pk}_{\mathcal{E}\mathcal{A}}) := \text{Setup}(1^\lambda)$
- $(\text{pk}_i, (\text{sk}_i, \text{pk}_i)) := \text{Register}\langle \mathcal{E}\mathcal{A}(\text{sk}_{\mathcal{E}\mathcal{A}}), \mathcal{V}_i() \rangle$
- $(\text{I}, \text{C}) :=$   
 $\text{SetupElection}(\text{sk}_{\mathcal{E}\mathcal{A}}, n, m, \text{params}, \text{Election-information})$
- $(\perp, (b_i, \pi_{b_i})) :=$   
 $\text{Vote}\langle \mathcal{E}\mathcal{A}(\text{sk}_{\mathcal{E}\mathcal{A}}), \mathcal{V}_i(c_i, \text{sk}_i), \text{params}, \text{pk}_{\mathcal{E}\mathcal{A}}, \text{pk}_i, \text{I}, \text{C}, \mathcal{B}\mathcal{B} \rangle$
- $\mathcal{B}\mathcal{B} \leftarrow \text{Cast}\langle \mathcal{B}\mathcal{B}(), \mathcal{V}_i(b_i, \pi_{b_i}) \rangle$
- $\{0, 1\} = \text{Valid}(\mathcal{B}\mathcal{B}, b)$
- $(\mathbf{T}, \pi_{\mathbf{T}}) := \text{Tally}(\text{sk}_{\mathcal{E}\mathcal{A}}, \text{params}, \text{C}, \mathcal{B}\mathcal{B})$
- $\{0, 1\} = \text{Verify}(\mathbf{T}, \text{params}, \text{pk}_{\mathcal{E}\mathcal{A}}, \mathcal{B}\mathcal{B}, \text{C}, \text{I}, b_i, \pi_{b_i}, \pi_{\mathbf{T}})$

# OPERATION I

$(\text{params}, sk_{\mathcal{EA}}, pk_{\mathcal{EA}}) := \text{Setup}(1^\lambda)$

- The EA generates the cryptographic parameters and its credentials

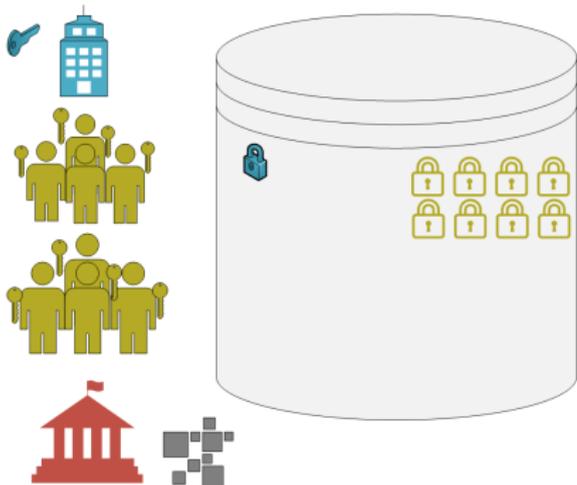


Setup

# OPERATION II

$$(pk_i, (sk_i, pk_i)) := \text{Register}\langle \mathcal{EA}(sk_{\mathcal{EA}}), \mathcal{V}_i() \rangle$$

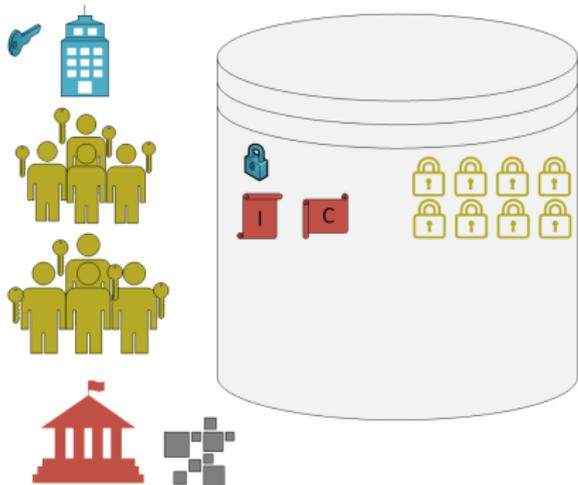
- Each voter registers with some identifying information and obtains some form of credentials



Register

$(I, C) := \text{SetupElection}(sk_{\mathcal{E}\mathcal{A}}, n, m, \text{params}, \text{Election-information})$

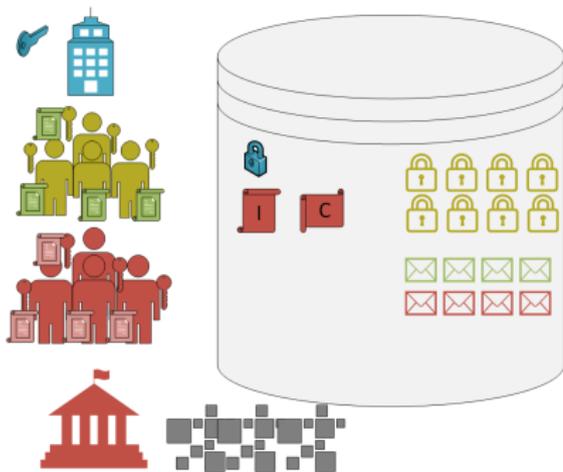
- $\mathcal{E}\mathcal{A}$  creates the election by publishing the list of eligible voters and candidates



## Voting: Vote and Cast functionalities

$$(\perp, (b_i, \pi_{b_i})) := \text{Vote}(\mathcal{EA}(\text{sk}_{\mathcal{EA}}), \mathcal{V}_i(c_i, \text{sk}_i), \text{params}, \text{pk}_{\mathcal{EA}}, \text{pk}_i, I, C, \mathcal{BB})$$
$$\mathcal{BB} \leftarrow \text{Cast}(\mathcal{BB}(), \mathcal{V}_i(b_i, \pi_{b_i}))$$

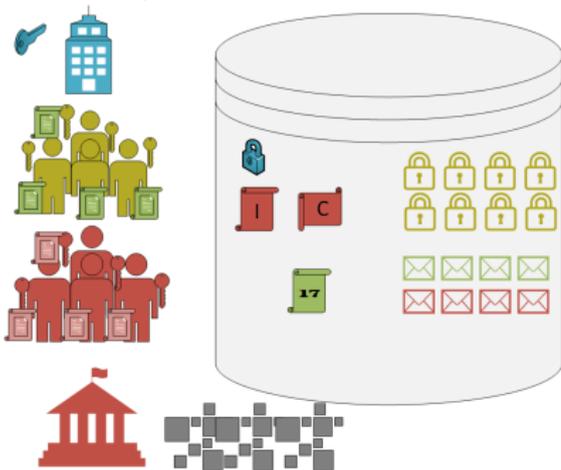
- The voter presents a credential and commits to a voting choice
- The EA verifies the right to vote
- The voter casts the ballot
- The validity of the ballot is checked



# OPERATION - V

$(\mathbf{T}, \pi_{\mathbf{T}}) := \text{Tally}(\text{sk}_{\mathcal{E}\mathcal{A}}, \text{params}, C, \mathcal{BB})$

- The EA tallies the votes
- Releases the result along with a proof of correctness
- Verification takes place



Tally

# ADVERSARIAL CAPABILITIES

## Motivation

The everlasting privacy adversary is not only confined to the public view of the election. It also has access to 'insider' information.

## Contemporary Adversary $\mathcal{A}$

- Computationally Constrained
- Active participation (through voter corruption)

## Future Adversary $\mathcal{A}'$

- Computationally Unbounded
- Weak Everlasting Privacy: Public protocol transcript
- Everlasting Privacy: Cooperate with  $\mathcal{A}$
- Strong Everlasting Privacy: communication and 'insider' data

# THE SECURITY GAME

- An extension of [BCG<sup>+</sup>15] for privacy
- $\mathcal{A}$  sees two Bulletin Boards
- $\mathcal{C}$  executes Setup, Register in both Boards
- $\mathcal{A}$  chooses the eligible voters and candidates to setup the election
- $\mathcal{A}$  dynamically corrupts voters and schedules voting
- Corrupted ballots go to both BBs
- Challenge phase:  $\mathcal{A}$  chooses two options  $c_0, c_1$  for honest in  $BB_0, BB_1$
- $\mathcal{C}$  performs tally
- $\mathcal{A}$  must guess board

# THE SECURITY GAME II

## Algorithm 1: Privacy Experiment $\text{Exp}_{\mathcal{A}, \Pi, t}^{\text{priv}, \beta}(1^\lambda, n, m)$

```
(params, skEA, pkEA) ← Π.Setup(1λ)
BBb ← (params, pkEA)  b ∈ {0, 1}
for i ∈ [n] do
  (ski, pki) ← Π.Register(EA(skEA), Vi)
  BBb ← pki  b ∈ {0, 1}
  Aux ← AuxRegister
end
(I, C) ← AΠ.SetupElection(n, m, BBb)  b ∈ {0, 1}
VC ← A(I, corrupt)
Vh := I \ VC
for i ∈ I do
  if i ∈ VC then
    ci ← A(choose)
    (bi, πbi) ← AΠ.Vote(ci, ski, BBb)  b ∈ {0, 1}
  else
    (c0, c1) ← A(choose)
    (bi0, πbi0) ←
      Vote((EA(skEA), Vi(c0, ski), BB0))
    (bi1, πbi1) ←
      Vote((EA(skEA), Vi(c1, ski), BB1))
  end
end
```

```
viewA ← viewVote
Aux ← AuxVote
for i ∈ I do
  if i ∈ VC then
    BBb ← AΠ.Cast(b'i, BBb)  b ∈ {0, 1}
  else
    BB0 ← Π.Cast(b'i0, BB0)
    BB1 ← Π.Cast(b'i1, BB1)
  end
end
viewA ← viewCast
Aux ← AuxCast
(T, πT) ← AΠ.Tally()
β' ← A(T, πT, BBβ, guess)
if β = β' ∧ |VC| ≤ t then
  | return 1
else
  | return 0
end
```

# WEAK EVERLASTING PRIVACY

---

**Algorithm 2:**  $\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{w-ever-priv}, \beta}(1^\lambda, n, m)$

---

```
(c0, c1) ←  $\mathcal{A}'()$ 
( $\mathcal{BB}_\beta, \mathbf{T}$ ) ←  $\mathcal{A}'^\Pi()$ 
 $\beta' \leftarrow \mathcal{A}'(\mathbf{T}, \pi_{\mathbf{T}}, \mathcal{BB}_\beta, \mathbf{guess})$ 
if  $\beta = \beta'$  then
  | return 1
else
  | return 0
end
```

---

## Weak Everlasting Privacy for $\Pi$

$\forall \mathcal{A}', \exists$  negligible function  $\mu : \forall n, m :$

$\Pr[\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{w-ever-priv}, 0}(1^\lambda, n, m)] -$

$\Pr[\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{w-ever-priv}, 1}(1^\lambda, n, m)] \leq \mu(\lambda)$

- Parameterization by voting scheme  $\Pi$  and future adversary  $\mathcal{A}'$
- $\mathcal{A}'$  selects the voting choices
- $\mathcal{A}'$  uses only the public view ( $\mathcal{BB}$ ) to distinguish voting behaviour
- Game-based version of practical everlasting privacy of [ACKR13]

# EVERLASTING PRIVACY

---

**Algorithm 3:**  $\text{Exp}_{\mathcal{A}', \mathcal{A}, \Pi, t}^{\text{ever-priv}, \beta}(1^\lambda, n, m)$

---

```
( $c_0, c_1, V_c$ )  $\leftarrow \mathcal{A}'()$ 
( $\mathcal{BB}_\beta, \text{view}_{\mathcal{A}}, T$ )  $\leftarrow \mathcal{A}'^{\Pi, \mathcal{A}}()$ 
 $\beta' \leftarrow \mathcal{A}'(T, \pi_T, \mathcal{BB}_\beta, \text{view}_{\mathcal{A}}, \text{guess})$ 
if  $\beta = \beta' \wedge |V_c| \leq t$  then
  | return 1
else
  | return 0
end
```

---

## Everlasting Privacy for $\Pi$

$\forall \mathcal{A}, \mathcal{A}', \exists$  negligible function  $\mu : \forall n, m :$

$\Pr[\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{ever-priv}, 0}(1^\lambda, n, m)] -$

$\Pr[\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{ever-priv}, 1}(1^\lambda, n, m)] \leq \mu(\lambda)$

- Parameterization by voting scheme  $\Pi$  and current and future adversaries  $\mathcal{A}, \mathcal{A}'$
- $\mathcal{A}'$  selects the voting choices and corruption strategies
- $\mathcal{A}'$  uses the public view ( $\mathcal{BB}$ ) and  $\mathcal{A}$  corruption information  $\text{view}_{\mathcal{A}}$  to distinguish voting behaviour

# STRONG EVERLASTING PRIVACY

---

**Algorithm 4:**  $\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{s-ever-priv}, \beta}(1^\lambda, n, m)$

---

```
( $c_0, c_1, V_c$ )  $\leftarrow \mathcal{A}'()$ 
( $\mathcal{BB}_\beta, \text{view}_{\mathcal{A}}, \text{Aux}, T$ )  $\leftarrow \mathcal{A}'^{\Pi, \mathcal{A}}(c_0, c_1)$ 
 $\beta' \leftarrow \mathcal{A}'(T, \pi_T, \mathcal{BB}_\beta, \text{view}_{\mathcal{A}}, \text{Aux}, \text{guess})$ 
if  $\beta = \beta' \wedge |V_c| \leq t$  then
  | return 1
else
  | return 0
end
```

---

## Strong Everlasting Privacy for $\Pi$

$\forall \mathcal{A}, \mathcal{A}', \exists$  negligible function  $\mu : \forall n, m :$

$\Pr[\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{s-ever-priv}, 0}(1^\lambda, n, m)] -$

$\Pr[\text{Exp}_{\mathcal{A}', \Pi, t}^{\text{s-ever-priv}, 1}(1^\lambda, n, m)] \leq \mu(\lambda)$

- Parameterization by voting scheme  $\Pi$  and current and future adversaries  $\mathcal{A}, \mathcal{A}'$
- $\mathcal{A}'$  selects the voting choices and corruption strategy
- $\mathcal{A}'$  uses the public view ( $\mathcal{BB}$ ) and  $\mathcal{A}$  corruption information  $\text{view}_{\mathcal{A}}$  to distinguish voting behaviour
- combines comms insider information  $\text{Aux}$

# EVERLASTING PRIVACY WITH PERFECTLY HIDING COMMITMENTS

- The problem: decommitments exchanged through private channels
- An insider will have access to them
- Commitment opening exchanged through private channel = encrypted ballot
- Strong everlasting privacy cannot be attained (in principle)
- At most weak everlasting privacy

# EVERLASTING PRIVACY WITH ANONYMOUS CHANNEL

The anonymous channel can:

- Nullify leaked information & casting order
- by disconnecting votes from voters
- can help achieve strong everlasting privacy
- must maintain other voting properties (verifiability, eligibility)
- Are we trading a problem for a different one?
- Information theoretical anonymity vs lack of central control
- Implementation on a large scale with such compromises



# REFERENCES

-  MYRTO ARAPINIS, VÉRONIQUE CORTIER, STEVE KREMER, AND MARK RYAN. **PRACTICAL EVERLASTING PRIVACY.** 2013.
-  BEN ADIDA. **HELIOS: WEB-BASED OPEN-AUDIT VOTING.** 2008.
-  DAVID BERNHARD, VÉRONIQUE CORTIER, DAVID GALINDO, OLIVIER PEREIRA, AND BOGDAN WARINSCHI. **SOK: A COMPREHENSIVE ANALYSIS OF GAME-BASED BALLOT**
-  JOSH BENALOH AND DWIGHT TUINSTRA. **RECEIPT-FREE SECRET-BALLOT ELECTIONS (EXTENDED ABSTRACT).** 1994.
-  RONALD CRAMER, MATTHEW FRANKLIN, BERRY SCHOENMAKERS, AND MOTI YUNG. **MULTI-AUTHORITY SECRET-BALLOT ELECTIONS WITH LINEAR WORK.** 1996.
-  DAVID CHAUM. **UNTRACEABLE ELECTRONIC MAIL, RETURN**
-  **PRIVACY WITHOUT INDIVIDUAL VERIFIABILITY.** 2018.
-  ÉDOUARD CUVELIER, OLIVIER PEREIRA, AND THOMAS PETERS. **ELECTION VERIFIABILITY OR BALLOT PRIVACY: DO WE NEED TO CHOOSE?** volume 8134 LNCS, 2013.
-  DENISE DEMIREL, J VAN DE GRAAF, AND R ARAÚJO. **IMPROVING HELIOS WITH EVERLASTING PRIVACY TOWARDS THE PUBLIC.** 2012.
-  **ZACHARAKIS, AND BINGSHENG ZHANG. TOWARDS EVERLASTING PRIVACY AND EFFICIENT COERCION RESISTANCE IN REMOTE ELECTRONIC VOTING.** 2019.
-  THOMAS HAINES AND CLÉMENTINE GRITTI. **IMPROVEMENTS IN EVERLASTING PRIVACY: EFFICIENT AND SECURE ZERO KNOWLEDGE PROOFS.** 2019.
-  ARI JUELS, DARIO CATALANO, AND MARKUS JAKOBSSON.
-  ZACHARIAS, AND BINGSHENG ZHANG. **END-TO-END VERIFIABLE ELECTIONS IN THE STANDARD MODEL.** 2015.
-  PHILIPP LOCHER AND ROLF HAENNI. **VERIFIABLE INTERNET ELECTIONS WITH EVERLASTING PRIVACY AND MINIMAL TRUST.** 2015.
-  PHILIPP LOCHER, ROLF HAENNI, AND RETO E. KOENIG. **COERCION-RESISTANT INTERNET VOTING WITH EVERLASTING**